

STANKO ŽERAJIĆ
DRAGAN CVETKOVIĆ
ILIJA MLADENOVIĆ

Faculty of Technology,
University of Niš,
Leskovac, Serbia

SCIENTIFIC PAPER

66.011:577+66.02/.09:519.876.5

MODELING AND SIMULATION OF THE BIOPROCESS WITH RECIRCULATION*

The bioprocess models with recirculation present an integration of the model of continuous bioreaction system and the model of separation system. The reaction bioprocess is integrated with separation the biomass, formed product, no consumed substrate or inhibitory substance. In this paper the simulation model of recirculation bioprocess was developed, which may be applied for increasing the biomass productivity and product biosynthesis, increasing the conversion of a substrate-to-product, mixing efficiency and secondary CO₂ separation.

The goal of the work is optimal bioprocess configuration, which is determined by simulation optimization. The optimal chemostat state was used as referent. Step-by-step simulation method is necessary because the initial bioprocess state is changing with recirculation in each step. The simulation experiment confirms that at the recirculation ratio $\alpha = 0.275$ and the concentration factor $C = 4$ the maximum glucose conversion to ethanol and at a dilution rate ten times larger.

The recirculation technique with separation is primarily used for the increase of bioprocess productivity for biomass synthesis, but it can also be applied for bioprocess efficiency increase for product synthesis as well as for the increase of the total substrate conversion into the product. Most frequently, the bioprocess is combined with the separator S for obtained biomass, product formed and non-consumed substrate.

At biomass production, the permanent inoculation of the fresh sterile medium, the maintenance of exponential growth phase or the achievement of biomass more than critical are provided by biomass recirculation. The application of the cell biomass recirculation at chemostat enables bioprocess progress in the conditions when the dilution rate D is considerably higher than the specific microbial growth rate μ [1].

Considering the fact that the biosystem functions with the dilution rate higher than the specific growth rate, the volumetric bioprocess productivity is increased. Furthermore, the increase of the cell concentration enables proportional increase of substrate consumption rate. The instability border of classical chemostat, which is because of cell washing from bioreactor connected to the condition $D \approx \mu$, during which the maximal bioprocess productivity, is changed towards higher values [2,3].

In this paper, the possibility of application of simulation optimization technique for improvement of configuration of bioprocess with recirculation is researched, with the aim to increase productivity and outlet ethanol concentration [4,5]. Simulation optimization aims at determining the best values of input parameters, given an output criterion. This approach allows a large variety of new types of problems to be solved, such as design of complex dynamic biosystems [6].

PROCESS MODELLING

The complex bioprocess was decomposed to the reaction-transformation and separation subsystem by using subsystem analysis. The bioprocess scheme is shown in Figure 1.

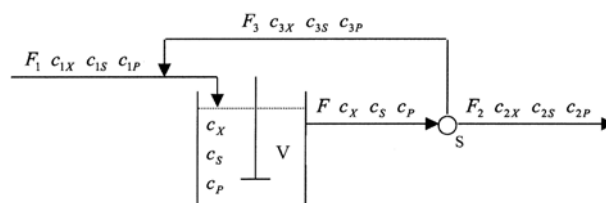


Figure 1. Scheme of the bioprocess with recirculation

Transformation process balance:

$$\frac{d(Vc_x)}{dt} = F_1c_{1X} + F_3c_{3X} + r_XV - Fc_x \quad (1)$$

$$\frac{d(Vc_s)}{dt} = F_1c_{1S} + F_3c_{3S} - r_SV - Fc_s \quad (2)$$

$$\frac{d(Vc_p)}{dt} = F_1c_{1P} + F_3c_{3P} + r_PV - Fc_p \quad (3)$$

$$\frac{dV}{dt} = F_1 + F_3 - F \quad (4)$$

*Rad saopšten na VII simpozijumu "Savremene tehnologije i privredni razvoj", Leskovac, 19. i 20. oktobar 2007. godine

Author address: S. Žerajic, University of Niš, Faculty of Technology, Bulevar oslobođenja 124, 16000 Leskovac, Serbia

E-mail: zerajic@yahoo.com

Paper received: July 31, 2007

Paper accepted: September 19, 2007

Separation process balance:

$$Fc_X - F_2c_{2X} - F_3c_{3X} = 0 \quad (5)$$

$$Fc_S - F_2c_{2S} - F_3c_{3S} = 0 \quad (6)$$

$$Fc_P - F_2c_{2P} - F_3c_{3P} = 0 \quad (7)$$

$$F - F_2 - F_3 = 0 \quad (8)$$

Initial conditions:

$$\begin{aligned} t = 0, c_X(0) = c_{X0}, c_S(0) = c_{S0}, \\ c_P(0) = 0, V = V_0 \end{aligned} \quad (9)$$

If in sterile inlet flow F_1 , only the limiting substrate with concentration c_{1S} ($c_{1X} = c_{1P} = 0$) is present, and if the recirculation flow F_3 is presented by recirculation ratio $\alpha = F_3/F_1$ based on volumetric flow rates, and the concentration in recirculation flow c_{3X} is expressed by concentration factor $C_X^{conc} = c_{3X}/c_X$, the model of reaction subsystem at constant volume, is reduced in the following equation system:

$$V \frac{dc_X}{dt} = \alpha F_1 \cdot c_X C_X^{conc} + r_X V - (1 + \alpha) F_1 \cdot c_X \quad (10)$$

$$V \frac{dc_S}{dt} = F_1 c_{1S} + \alpha F_1 \cdot c_S - r_S V - (1 + \alpha) F_1 \cdot c_S \quad (11)$$

$$V \frac{dc_P}{dt} = \alpha F_1 \cdot c_P + r_P V - (1 + \alpha) F_1 \cdot c_P \quad (12)$$

$$\frac{dV}{dt} = 0 \quad (13)$$

Initial conditions:

$$\begin{aligned} t = 0, c_X(0) = c_{X0} = 0, c_S(0) = c_{S0}, \\ c_P(0) = 0, V = V_0 \end{aligned} \quad (14)$$

The border bioprocess models with recirculation are generated for the biomass production process with complete biomass separation and recirculation (Model 1), for the process with complete substrate separation and recirculation with the goal of getting the total substrate conversion (Model 2) and for the process with complete separation of the inhibitory product, with the goal of the maximum substrate conversion and process productivity (Model 3).

Model 1. The biomass is completely separated in the separator and returns in the bioprocess by the flow F_3 (condition: $F_3c_{3X} = Fc_X$, $c_{3S} = 0$, $c_{3P} = 0$), and outlet reaction mixture (reactant and product) leaves the separator by the flow F_2 (condition: $c_{2X} = 0$, $c_{2S} = c_S$, $c_{2P} = c_P$),

$$\frac{d(Vc_X)}{dt} = r_X V$$

$$\frac{d(Vc_S)}{dt} = F_1 c_{1S} - r_S V - F c_S$$

$$\frac{d(Vc_P)}{dt} = r_P V - F c_P$$

$$dV/dt = F_1 + F_3 - F$$

Initial conditions:

$$\begin{aligned} t = 0, c_X(0) = c_{X0} = 0, c_S(0) = c_{S0}, \\ c_P(0) = 0, V = V_0 \end{aligned}$$

Model 2. The substrate that has not reacted is separated in the separator and returned into the bioprocess by flow F_3 (condition: $F_3c_{3S} = Fc_S$, $c_{3X} = 0$, $c_{3P} = 0$), and outlet reaction mixture (biomass and product) leaves the separator by flow F_2 (condition: $c_{2X} = c_X$, $c_{2S} = 0$, $c_{2P} = c_P$),

$$\frac{d(Vc_X)}{dt} = r_X V - F c_X$$

$$\frac{d(Vc_S)}{dt} = F_1 c_{1S} - r_S V$$

$$\frac{d(Vc_P)}{dt} = r_P V - F c_P$$

$$dV/dt = F_1 + F_3 - F$$

Initial conditions:

$$\begin{aligned} t = 0, c_X(0) = c_{X0} = 0, c_S(0) = c_{S0}, \\ c_P(0) = 0, V = V_0 \end{aligned}$$

Model 3. The formed product is separated in the separator and is taken away by the flow F_2 (condition: $F_2c_{2P} = Fc_P$, $c_{2X} = 0$, $c_{2S} = 0$), and outlet reaction mixture (biomass and substrate) is returned in the bioprocess by flow F_3 (condition: $F_3c_{3X} = Fc_X$, $F_3c_{3S} = Fc_S$, $c_{3P} = 0$)

$$\frac{d(Vc_X)}{dt} = r_X V$$

$$\frac{d(Vc_S)}{dt} = F_1 c_{1S} - r_S V$$

$$\frac{d(Vc_P)}{dt} = r_P V - F c_P$$

$$dV/dt = F_1 + F_3 - F$$

Initial conditions:

$$\begin{aligned} t = 0, c_X(0) = c_{X0} = 0, c_S(0) = c_{S0}, \\ c_P(0) = 0, V = V_0 \end{aligned}$$

By including the relations for recirculation ratio α and concentrating factor C_X^{conc} , and by expressing the volumetric reaction rates (r_X , r_S , r_P) with suitable specific reaction rates (μ , v_S , v_P), the models of reaction subsystem Model 1–3 are transformed in the following form:

Model 1.1. The biomass is completely separated in the separator and is returned into the bioprocess, and outlet reaction mixture (reactant and product) leaves the separator by the flow F_2 (condition: $F_3c_{3X} = Fc_X$)

$$V \frac{dc_X}{dt} = r_X V = c_X \mu V$$

$$V \frac{dc_S}{dt} = F_1 c_{1S} - r_S V - (1 + \alpha) F_1 \cdot c_S =$$

$$= F_1 c_{1S} - c_X v_S V - (1 + \alpha) F_1 \cdot c_S$$

$$V \frac{dc_P}{dt} = r_P V - (1 + \alpha) F_1 \cdot c_P =$$

$$= c_X v_P V - (1 + \alpha) F_1 \cdot c_P$$

$$dV/dt = 0$$

Initial conditions:

$$t = 0, c_X(0) = c_{X0} = 0, c_S(0) = c_{S0}, c_P(0) = 0, V = V_0$$

Model 2.1. The substrate that has not reacted is separated in the separator and is returned into the bioprocess, and the outlet reaction mixture (biomass and product) leaves the separator by flow F_2 (condition: $F_3 c_{3S} = F c_S$)

$$V \frac{dc_X}{dt} = r_X V - (1 + \alpha) F_1 \cdot c_X = c_X \mu V - (1 + \alpha) F_1 \cdot c_X$$

$$V \frac{dc_S}{dt} = F_1 c_{1S} - r_S V = F_1 c_{1S} - c_X v_S V$$

$$V \frac{dc_P}{dt} = r_P V - (1 + \alpha) F_1 \cdot c_P = c_X v_P V - (1 + \alpha) F_1 \cdot c_P$$

$$dV/dt = 0$$

Initial conditions:

$$t = 0, c_X(0) = c_{X0} = 0, c_S(0) = c_{S0}, c_P(0) = 0, V = V_0.$$

Model 3.1. The formed product is separated in the separator and is taken away by flow F_2 , and the outlet reaction mixture (biomass and substrate) is back in the bioprocess (condition: $F_2 c_{P2} = F c_P$),

$$V \frac{dc_X}{dt} = r_X V = c_X \mu V$$

$$V \frac{dc_S}{dt} = F_1 c_{1S} - r_S V = F_1 c_{1S} - c_X v_S V$$

$$V \frac{dc_P}{dt} = r_P V - (1 + \alpha) F_1 \cdot c_P = c_X v_P V - (1 + \alpha) F_1 \cdot c_P$$

$$dV/dt = 0$$

Initial conditions:

$$t = 0, c_X(0) = c_{X0} = 0, c_S(0) = c_{S0}, c_P(0) = 0, V = V_0.$$

KINETIC MODEL

The kinetic model is semi-empirical, non-structured from the aspect of cell composition and distributed from the aspect of biomass quantification according as total concentration of biomass, which is uniform distribution at volume of fluid culture.

The kinetic model is generated from mixed semi-empirical biomass growth model, which includes modified non-competitive substrate inhibition and linear product inhibition.

$$r_X = \frac{dc_X}{dt} = c_X \cdot \frac{\mu_m \cdot c_S}{K_M + C_S + \frac{c_S^2}{K_{2S}}} \cdot \left(1 - \frac{c_P}{P_m}\right) - m \cdot c_X \quad (15)$$

$$-r_S = \frac{dc_S}{dt} = c_X \cdot \frac{v_{ms} \cdot c_S}{K_M + C_S + \frac{c_S^2}{K_{IS}}} \cdot \left(1 - \frac{c_P}{P_{mm}}\right) \quad (16)$$

$$r_P = \frac{dc_P}{dt} = c_X \cdot \frac{v_{mp} \cdot c_S}{K_M + c_S + \frac{c_S^2}{K_{1S}}} \cdot \left(1 - \frac{c_P}{P_{mm}}\right) \quad (17)$$

The empirical model parameters P_m and P_{mm} are determined in the independent experiment. They represent the corresponding ethanol concentrations, at which cell growth and ethanol synthesis stopped respectively. From a biochemical aspect these parameters represent the biological switching effect, which is a specific characteristic of the cell culture *Saccharomyces cerevisiae*.

The experimental data from kinetic experiments was used for kinetic parameter estimation. The model parameters were calculated based on the ordinary least squared method. The Levenberg-Marquardt iterative fitting method is used at parameter estimation [7,8]. The model validity is statistically estimated by Fischer's test and preliminary by correlation coefficient. The results of the statistical test presented in Table 1, show good comparison of the experimental and simulation data.

Table 1. The kinetic model Eqs. (15–17) parameter estimation, for different initial substrate concentration ($c_{S0} = 50–250 \text{ g dm}^{-3}$, $c_{X0} = 0.75 \text{ g dm}^{-3}$, $P_m = 84$, $P_{mm} = 95$)

c_{S0}	μ_m	v_{ms}	v_{mp}	K_M	K_{IS}	F_{calc}^{tot}	F_{lab}	r_{cor}
50	0.272	2.603	1.224	1.393	401.800	0.105	2.484	1.000
100	0.229	2.380	1.104	0.688	422.300	0.043	2.084	1.000
150	0.195	2.434	1.069	1.764	470.800	0.472	1.841	0.999
200	0.181	1.972	0.815	4.560	239.900	0.277	1.592	0.999
250	0.116	1.376	0.543	8.917	361.700	0.335	1.278	1.000

RESULTS AND DISCUSSION

Analysis of the bioprocess with recirculation

The simulation model of bioprocess with recirculation flow obtained from Eqs. (1–8), is analyzed for different conditions of the separation subsystem. The bioprocess with recirculation flow represents an integration of continual flow reaction system and separation system. The recirculation technique represents permanent inoculation of the reaction subsys-

tem that excludes the need to produce the starter culture all through the process.

The shortage of this bioprocess configuration is in time accumulation of metabolites in reaction subsystem and in engineering problems of realization of the setting separation degree in the separation subsystem.

Analyzing the reaction–separation model, the main contribution of bioprocess with recirculation flow can be confirmed. The model is derived under the presumption that the inlet flow is sterile, and that the bioprocess is initialized by an impulse injection of biomass at the start of the process, which is realized in the model by specifying the zero inlet biomass concentration $C_{1X} = 0$ in inlet flow F_1 , i.e. c_{X0} as the initial condition that is the mathematically formalized impulse biomass injection.

$$V \frac{dc_X}{dt} = \alpha F_1 \cdot c_X C_X^{k_{onc}} + r_X V - (1 + \alpha) F_1 \cdot c_X \quad (18)$$

$$V \frac{dc_S}{dt} = F_1 c_{1S} + \alpha F_1 \cdot C_S - r_S V - (1 + \alpha) F_1 \cdot c_S \quad (19)$$

$$V \frac{dc_P}{dt} = \alpha F_1 \cdot c_P + r_P V - (1 + \alpha) F_1 \cdot c_P \quad (20)$$

$$dV/dt = 0 \quad (21)$$

Initial conditions:

$$\begin{aligned} t = 0, c_X(0) = c_{X0} = 0, c_S(0) = c_{S0}, \\ c_P(0) = 0, V = V_0 \end{aligned} \quad (22)$$

In steady–state conditions, the model of biomass forming is transformed in the following form:

$$\frac{1}{V} (\alpha F_1 \cdot c_X C_X^{k_{onc}} + r_X V - (1 + \alpha) F_1 \cdot c_X) = 0 \quad (23)$$

By introduction of the specific growth rate $r_X = \mu c_X$ in Eq. (23) it follows,

$$D = \frac{F_1}{V} = \frac{\mu}{1 + \alpha - \alpha C_X^{k_{onc}}} \quad (24)$$

that represents the function of dilution rate D from the specific growth rate μ , recirculation ratio α and concentrating factor $C_X^{k_{onc}}$.

The Eq. (24) shows that the dilution rate is higher than the specific growth rate in the process. The concentrating factor is much higher than one, $C_X^{k_{onc}} \gg 1$, and the recirculation ratio is lower than one, $\alpha \ll 1$, so that the denominator of the equation is less than one. In the chemostat with cell recirculation, the cell concentration is $(1/1 + \alpha - \alpha C_X^{k_{onc}})$ times higher compared to the standard chemostat.

With the research of the bioprocess with recirculation, the control values, such as inlet flows and their corresponding concentrations are changing. The values of the recirculation flow, main flow and concentrations are also changed, depending on the

concentration factor and recirculation ratio. These changes lead to changes of initial values of the reaction subsystem state and that leads to change of the kinetic parameter values.

In each time interval (t_i, t_{i+1}) , which is determined by simulation step Δt , the simulated process state variables in time t_i , will be the initial condition for simulation in time t_{i+1} . Therefore, in each simulation step, the values of kinetic parameters with values of changeable states will change, especially with the actual concentration of limiting substrate.

The module for the specification of control values (input variable), components with kinetic model, corresponding simulation algorithm and components for simulated response show constitute the basic structure of the process simulation model. In addition, the component with the model for the determining of the values of the kinetic parameter models in the function of the initial concentration of limiting substrate is included.

Simulation of the bioprocess with recirculation

In development of the software applications, object oriented transformation method was used. The objects of complex bioprocess are modeled by heterogeneous program packages. This development dynamics of the engineering program packages are directly incorporated in software applications. Program components were generated with MathCAD program package [9]. The new generating program components were integrated in Mathconnex environment. Matconnex is a stable explorer for visual integration of heterogeneous program packages for creation of the continual simulation [10]. The process is simulated on the process simulation model, with kinetic model Eqs. (15–17) and with confirmed parameters of the kinetic model from Table 1. The structure of the simulation software is shown in Figure 6.

The simulation software of the process with recirculation, consist of three basic components: "TRANSFORMATION PROCESS", "SEPARATION PROCESS" and "VARIABILITY KINETIC PARAMETERS" component for estimation of variable values of the kinetic parameters in the function of the reaction subsystem state change.

The input simulator system is consisted of a module for specification of the starting conditions in reaction subsystem "INITIAL CONDITIONS", the module for volumetric flow specification "FLOW" and special modules for component concentration specification in input flow F_1 and recirculation flow F_3 .

The output simulator subsystem is specially separated for reaction subsystem and shown by the graph "REACTOR DYNAMICS", and the graphs "VOLUME" and "BIOMASS" are also shown because of the clarity.

The time changes of the concentration of biomass, glucose, ethanol and reaction subsystem values in the reactor i.e. output flow F are shown in the corresponding graphs.

The graphs "SEPARATOR DYNAMICS" and "BIOMASS DYNAMICS" show concentration changes of biomass, glucose and ethanol at the exit of the separator S in flow F_2 . These changes in flow F_2 are at the same time total response time changes of the state of the bioprocess with recirculation.

In the component "SEPARATION PROCESS" the predefined value of the concentrating factor (CF)

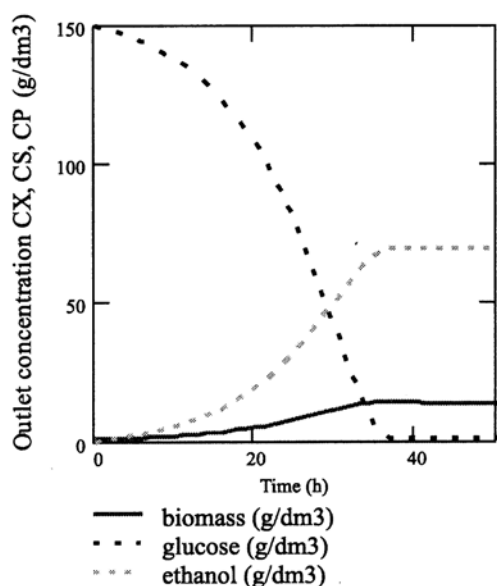


Figure 2. The simulation of the chemostat on the bioprocess simulation model with separation and biomass recirculation ($D = 0.02 \text{ h}^{-1}$, $\alpha = 0$, $C_X^{k_{onc}} = 1$).

is set, for example biomass on Figure 2, from which the biomass concentration is defined and the models for separation of substrate and product are introduced, Eqs. (5–8). The dilution rate is defined from the input flow F_1 and the effective reaction volume and according to Eq. (24) the values of the possible dilution rate above the values of the specific biomass growth rate is estimated, and this is comparatively used in relation to the standard chemostat.

The simulation software is transformed in the simulator of steady state chemostat in the testing phase by the appropriate flow choice ($F_3 = 0$, $F_1 = F_2 = 0.2 \text{ dm}^3 \text{ h}^{-1}$) and their content and by additional defining of the separation ratio ($c_{3X} = CX$, $c_{3S} = CS$ i $c_{3P} = CP$). Considering the effect of cell washing by continual flow trough chemostat, it can be supposed that the culture is permanently in the phase of exponential growth, so, in the kinetic model, the maintenance coefficient of biomass m can be approximation neglected $m = 0$. During the simulation, the maximum dilution rate limited by the washing effect and corresponding bioprocess state are defined.

At dilution rate $D = 0.02 \text{ h}^{-1}$ and by excluding of the separation subsystem from the simulation, by the condition $c_{3X} = CX$, $c_{3S} = CS$ i $c_{3P} = CP$, after 40 h of non-steady state, the process gets into quasi-steady state when the maximum biomass concentration $CX = 10.327 \text{ g dm}^{-3}$, ethanol $CP = 69.979 \text{ g dm}^{-3}$ and maximum conversion, i.e. minimum glucose output $CS = 1.587 \text{ g dm}^{-3}$. The simulation chemostat response got on the simulation software for bioprocess with recirculation is shown on Figure 2. At dilution rate $D = 0.2 \text{ h}^{-1}$ chemostat washing occurs.

In Figure 3, the biomass dynamics in reaction and separation subsystem, is comparatively presented for chemostat and the process with recirculation. The

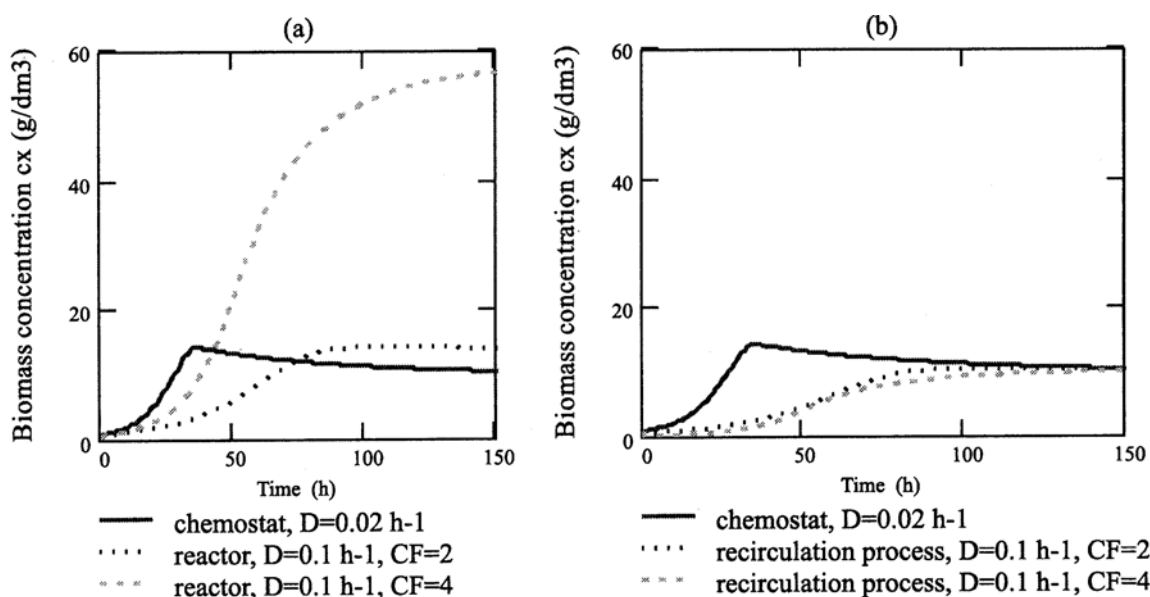


Figure 3. Biomass dynamics at the outlet of the reactor (a) and the separator (b)

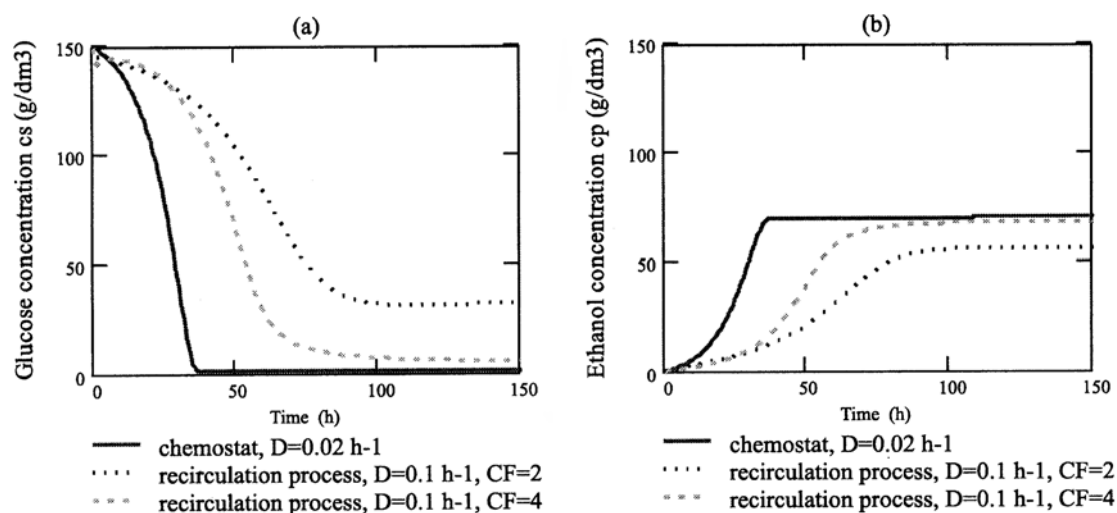


Figure 4. Dynamics of glucose (a) and ethanol (b) in recirculation bioprocess

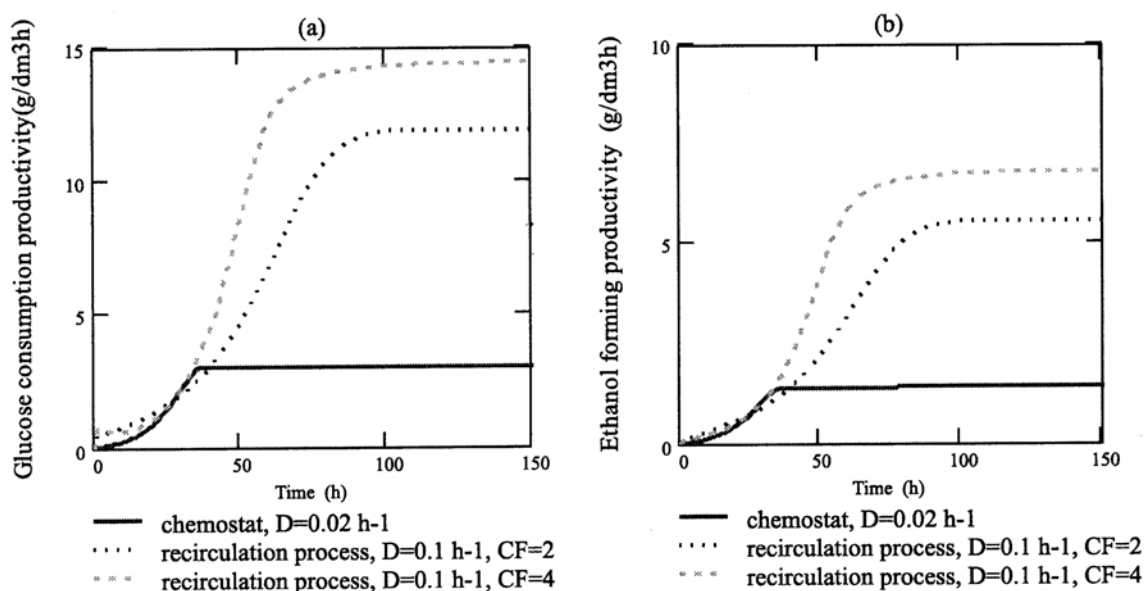


Figure 5. The productivity of glucose consumption (a) and ethanol forming (b)

simulation response obtained at the dilution rate $D = 0.02 \text{ h}^{-1}$. The process with recirculation is simulated at the dilution rate $D = 0.10 \text{ h}^{-1}$, at recirculation rate $\alpha = 0.275$ and concentration factors $CF = 2$ i $CF = 4$.

The corresponding changes of the concentrations of glucose and ethanol are shown in Figure 4.

The main aim of the recirculation, the productivity increase of the glucose consumption and ethanol forming is comparatively illustrated in Figure 5 for chemostat and recirculation bioprocess with different concentration factors.

In Figure 3, the bioprocess simulation with recirculation at recirculation ratio $\alpha = 0.275$ and concentrating factor $C_X^{conc} = 4$ is shown. At dilution rate of $D = 0.2 \text{ h}^{-1}$ at the output from the reaction subsystem of quasi-steady state values are: $C_X = 56.686 \text{ g dm}^{-3}$, $C_S = 5.585 \text{ g dm}^{-3}$ and $C_P = 68.164 \text{ g dm}^{-3}$ and they

are obtained after 70 h of non-steady state process. At the same time, the corresponding values at the separator output or with inlet flow F_2 from the total process are: $C_X = 9.926 \text{ g dm}^{-3}$, $C_S = 5.576 \text{ g dm}^{-3}$ and $C_P = 68.169 \text{ g dm}^{-3}$. Almost theoretical glucose conversion and maximum ethanol concentration are obtained at a ten times higher dilution rate.

The initial conditions specified by the input module "INITIAL CONDITIONS" ($V = 10 \text{ dm}^3$, $C_X = 0.75 \text{ g dm}^{-3}$, $C_S = 150 \text{ g dm}^{-3}$, $C_P = 0 \text{ g dm}^{-3}$) are used for both the chemostat and the process with recirculation of separated biomass simulation.

Kinetic and inhibitory model parameters in the form of specific values, at different initial biomass concentration and initial substrate concentration $c_{S0} = 150 \text{ g dm}^{-3}$ are obtained with the method of initial rates. Fischer's test confirms good agreement

with the experimental data (Table 2). The parameter values from Table 2 show the relative stability and small variations with the biomass concentration change. However, the changes of parameter values with the change of substrate concentration (Table 1) are

important. Therefore, the component "VARIABILITY KINETIC PARAMETERS" is integrated in the process simulator, to predict the kinetic parameter values with the change of process state in each step of the simulation.

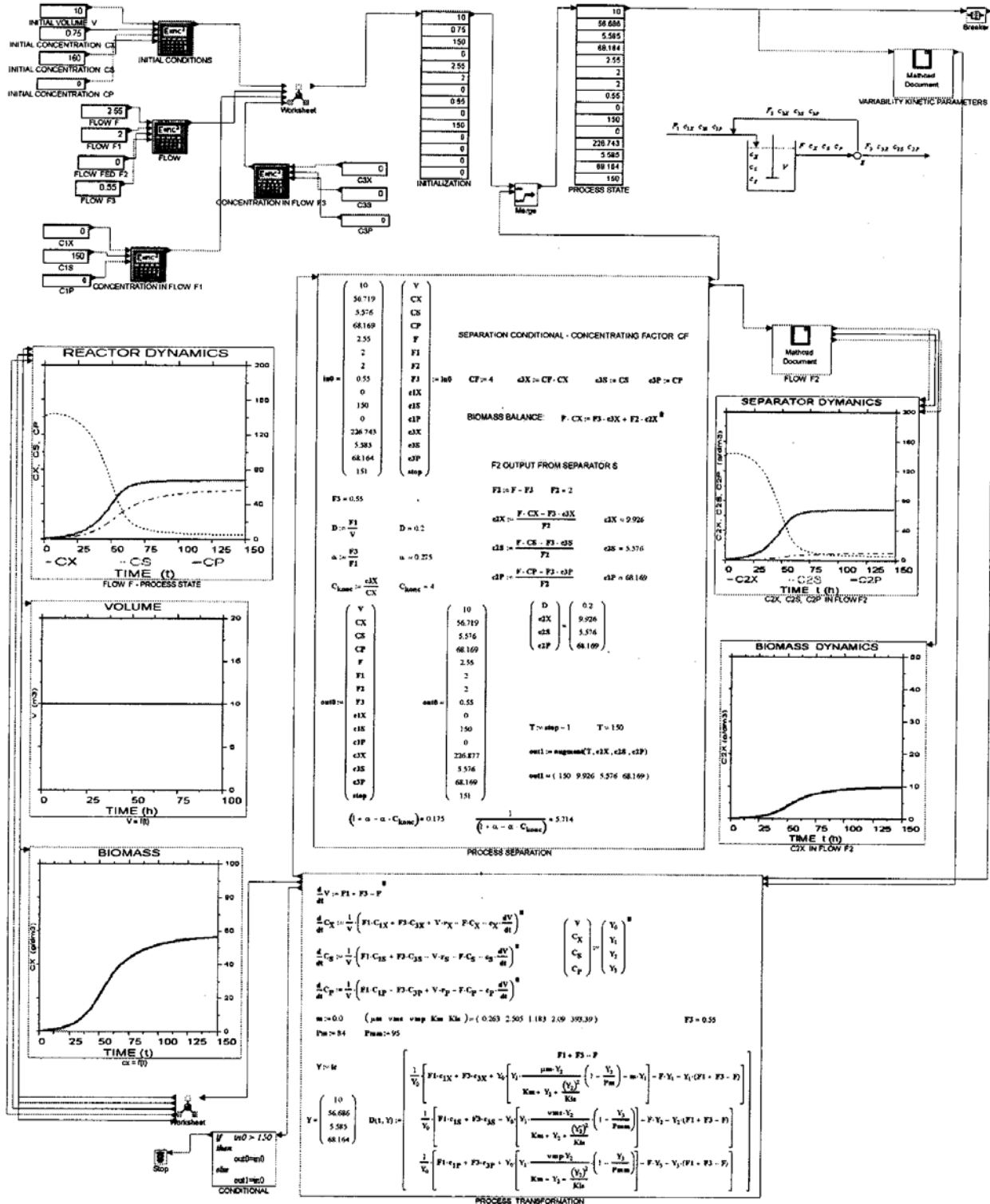


Figure 6. The simulation of flow bioprocess with separation and biomass recirculation, at dilution rate $D = 0.2 h^{-1}$, recirculation ratio $\alpha = 0.275$ and concentrating factor $C_X^{conc} = 4$.

Table 2. The kinetic model Eqs. (15–17) parameter estimation, for different initial biomass concentration ($c_{S0} = 150 \text{ g dm}^{-3}$, $P_m = 84$, $P_{mm} = 95$)

c_{X0}	μ_m	v_{ms}	v_{mp}	K_M	K_{IS}	F_{rac}^{tot}	F_{lab}	r_{cor}
0.75	0.196	2.433	1.069	1.756	471.2	0.518	1.861	0.999
1.50	0.185	2.519	1.100	1.882	395.2	0.057	1.984	1.000
3.00	0.192	2.423	1.058	1.088	450.2	0.069	2.168	1.000
9.00	0.181	2.407	1.057	1.855	529.6	0.033	2.818	1.000
15.00	0.173	2.275	0.998	1.238	814.0	0.029	3.179	1.000

At recirculation steady state process (Figure 5) the high productivity and conversion values are achieved. At outlet ethanol concentration $c_P = 57.719 \text{ g dm}^{-3}$ the coefficient of ethanol yield is $Y_{P/S} = 0.387$. At the same time the degree of glucose conversion into biomass and ethanol is 0.936. The theoretical ethanol yield in the absence of cell growth is $Y_{P/S} = 0.511$.

The separation and biomass recirculation techniques increase biomass concentration in the reaction subsystem, which enables bioprocess progress with almost theoretical yield and ethanol concentration and total glucose conversion, at dilution rates that are ten times higher compared to the ones with chemostat.

CONCLUSION

The computer-aided modeling and bioprocess simulation enable optimal bioprocess configuration with recirculation flow. The subsystem analysis and compartment approach at modeling enable independent development and testing of simulation software for reaction and separation process. The process simulator is formed by integration of operational simulators. The function of the classical chemostat can be simulated by appropriate choice of control values, e.g. by excluding separation process. The obtained values of the steady-state chemostat quantities are used as referential values.

The optimal values of chemostat productivity are limited by the cell-washing phenomenon. This limitation leads to relatively low steady-state cell concentration in chemostat, which results in low output ethanol concentration. The optimal values cannot be increased above the values obtained by optimization of the nutrient medium and process parameters, e.g. temperature, pH values and mixing. The optimal values of chemostat state are $c_X = 10.327 \text{ g dm}^{-3}$, $c_S = 1.587 \text{ g dm}^{-3}$ and $c_P = 69.979 \text{ g dm}^{-3}$, and they are obtained at dilution rate $D = 0.02 \text{ h}^{-1}$.

The separation subsystem, which is realized by centrifuge, increases the cell concentration that continually returns into the reaction subsystem by partial recirculation flow. The concentrating factor is also limited by centrifugal efficiency and recirculation flow techniques.

At concentrating degree $C_X^{k_{onc}}$ and recirculation ratio $\alpha = 0.275$, the dilution rate that enables the complete substrate conversion is determined ($D = 0.2$) by simulation optimization. The quasi-steady state of reaction subsystem ($c_X = 56.686 \text{ g dm}^{-3}$, $c_S = 5.585 \text{ g dm}^{-3}$, $c_P = 68.164 \text{ g dm}^{-3}$) shows considerably higher biomass concentration at the same time. The total recirculation flow effect is shown by simulation output from the separator ($c_X = 9.926 \text{ g dm}^{-3}$, $c_S = 5.576 \text{ g dm}^{-3}$ and $c_P = 68.169 \text{ g dm}^{-3}$). With almost total conversion of glucose, the dilution rate in the process with recirculation flow is almost ten times higher. At the same time, the bioprocess productivity proportionally increases as well.

The ratio of chemostat productivity $DP_1 = 1.363 \text{ g dm}^{-3} \text{ h}^{-1}$ and bioprocess with recirculation $DP_2 = 13.634 \text{ g dm}^{-3} \text{ h}^{-1}$, confirms the effectiveness of the applied method. The application of simulation optimization is an efficient approach that enables the configuration of complex bioprocess with the aim to increase productivity. The high productivity and output ethanol concentration considerably decreases ethanol separation expenses in the rectification phase.

NOMENCLATURE

c_X, c_S, c_P	g dm^{-3}	cell, substrate and product concentration in reaction subsystem
c_X, c_S, c_P	g dm^{-3}	cell, substrate and product concentration in reaction subsystem
c_{1X}, c_{1S}, c_{1P}	g dm^{-3}	cell, substrate and product concentration in inlet flow F_1
c_{2X}, c_{2S}, c_{2P}	g dm^{-3}	cell, substrate and product concentration in outlet flow F_2
c_{3X}, c_{3S}, c_{3P}	g dm^{-3}	cell, substrate and product concentration in flow F_3
c_{3X}, c_{3S}, c_{3P}	g dm^{-3}	cell, substrate and product concentration in recirculation flow F_3
$C_X^{k_{onc}}$	–	concentrating factor (CF)
D	h^{-1}	dilution rate
F_1, F_2, F_3	$\text{dm}^{-3} \text{ h}^{-1}$	inlet, outlet and recirculation flow
F_{calc}^{tot}	–	total Fisher's calculated values for validation test
K_M	g dm^{-3}	Monod's constant of cells growth rate
K_{IS}	g dm^{-3}	inhibition constant for noncompetitive inhibition by substrate
K_{IP}	g dm^{-3}	inhibition constant for competitive inhibition by product
m	$\text{g dm}^{-3} \text{ h}^{-1}$	maintenance coefficient for cells growth
P_m	g dm^{-3}	ethanol concentration that stops cell growth
P_{mm}	g dm^{-3}	ethanol concentration that stops ethanol biosynthesis
r_X	$\text{g dm}^{-3} \text{ h}^{-1}$	rate of growth (production) of cells related to glucose
r_S	$\text{g dm}^{-3} \text{ h}^{-1}$	rate of substrate consumption
r_P	$\text{g dm}^{-3} \text{ h}^{-1}$	rate of product formation

r_N	$g_X dm^{-3} h^{-1}$	rate of growth (production) of cells related to nitrogen
r_{cor}	–	correlation coefficient
V	dm^3	reaction subsystem volume

GREEK SYMBOLS

α	–	recirculation ratio
μ_m	$g_X g_X^{-1} h^{-1}$	maximum specific growth rate
v_S	$g_S g_X^{-1} h^{-1}$	specific rate of substrate consumption
v_{ms}	$g_S g_X^{-1} h^{-1}$	maximum specific rate of substrate consumption
v_P	$g_P g_X^{-1} h^{-1}$	specific rate of product formation
v_{mp}	$g_P g_X^{-1} h^{-1}$	maximum specific rate of product formation

REFERENCES

- [1] A.T. Jackson, Process Engineering in Biotechnology, Open University Press, Manchester, 1990, p. 111.
- [2] M.L. Shuler, F. Kargi, Bioprocess Engineering, Prentice Hall PTR, USA, 2002, p. 248.
- [3] J.E. Bailey, D.F. Olis, Biochemical Engineering Fundamentals, McGraw-Hill, New York, 1986, p. 539.
- [4] S. Andradottir, Simulation Optimization, In: Handbook of Simulation, J. Banks, ed., John Wiley and Sons, New York, 1998 307.
- [5] M.C. Fu, Ann. Operational Res. **53** (1994) 199.
- [6] H. Pierrival, J.L. Paris, Simulation Modelling Practice and Theory **11** (2003) 5.
- [7] K. Levenberg, Q. Appl. Math. **2** (1944) 164.
- [8] D. Marquardt, S.I.A.M. J. Appl. Math. **11** (1963) 431.
- [9] Mathcad User Manual Guide, Mathsoft, Massachusetts, 1997.
- [10] Mathconnex Getting Started, Mathsoft, Massachusetts, 1997.

IZVOD

MODELOVANJE I SIMULACIJA BIOPROCESA S POVRATNIM TOKOM

(Naučni rad)

Stanko Žerajić, Dragan Cvetković, Ilija Mladenović

Tehnološki fakultet, Univerzitet u Nišu, Bulevar oslobođenja 124, 16000 Leskovac, Srbija

Modeli bioprocasa s povratnim tokom predstavljaju integraciju modela kontinualnog bioreakcionog sistema i modela separacionog sistema. Reakcioni bioproces se integriše sa separacijom biomase, nastalog proizvoda, neproreagovanog supstrata ili inhibitorne supstance. U radu je razvijen simulacioni model recirkulacionog bioprocasa, koji se može primeniti za povećanje produktivnosti biomase i biosinteze proizvoda, povećanje konverzije supstrata u proizvod, efikasnosti mešanja i izdvajanja sporednog CO₂.

Cilj rada je optimalna konfiguracija bioprocasa s recirkulacijom koja se nalazi simulacionom optimizacijom. Optimalno stanje hemostata korišćeno je kao referentno. Simulacija korak-po-korak je neophodna metoda jer se početno stanje bioprocasa s recirkulacijom menja u svakom koraku simulacije. Simulacioni eksperiment potvrđuje da se pri recirkulacionom odnosu $\alpha = 0.275$ i faktoru koncentrovanja $C = 4$ postiže maksimalna konverzija glukoze u etanol i pri 10 puta većoj brzini razređenja.

Ključne reči: Bioproces sa recirkulacijom • Modelovanje i simulacija • Optimizacija simulacijom •

Key words: Bioprocess with recirculation • Modeling and simulation • Simulation optimization •