HEAT TRANSFER UNDER A PULSED SLOT TURBULENT IMPINGING JET AT LARGE TEMPERATURE DIFFERENCES

by

Peng XU a*, Arun S. MUJUMDAR b, Hee Joo POH c, and Boming YU d

a Institute of Surface Physics, College of Science, China Jiliang University, Hangzhou, P. R. China
b Department of Mechanical Engineering, National University of Singapore, Singapore
c Fluid Dynamics Division, Institute of High Performance Computing, Singapore
d School of Physics, Huazhong University of Science and Technology, Wuhan, P. R. China

Original scientific paper
UDC: 536.25:662.98
DOI: 10.2289/TSCI1001271X

Pulsed impinging jets have received increasing interest for their potential in heat and mass transfer enhancement. However, published results on effects of pulsations under different flow and geometrical parameters have shown conflicting results. To further understand the flow and thermal processes in pulsed impinging jets, a numerical investigation has been performed on a two-dimensional pulsed turbulent impinging jet under large temperature differences between the jet flow and the impinging surface to examine the effect of temperature-dependent thermophysical properties along with pulsation of the jet on the local Nusselt number distribution on the target surface. The numerical results show that the local time-averaged Nusselt numbers calculated with various thermal property values at the jet, film and impingement surface temperatures differ significantly for large temperature difference cases (>100 K). A parametric study for both heating and cooling cases indicates that no obvious enhancement by single sinusoidal pulsation can be found under current conditions except for cases with large temperature differences at distances far from stagnation point, i.e. in the wall jet region.

Key words: pulsed impinging jet, sinusoidal pulsation, heat transfer, Nusselt number

Introduction

Jet impingement has been commonly used in a great number of major industrial areas for various cooling, heating, and drying purposes due to their high convective heat transfer coefficients. Its industrial applications include thermal drying of continuous sheets of materials (e.g., textiles, films, papers, veneer, lumber, etc.) and foodstuff productions, electronic component and gas turbine cooling, manufacture of printed wiring boards and metal sheet, printing processes, deicing or aircraft wings and tempering of glass and non-ferrous metal sheets. Over the past several decades, extensive studies have been conducted on heat and mass transfer characteristics in impinging jets [1–4]. Previous studies have mainly focused on optimizing transport
processes associated with steady impinging jets. Recently, pulsed impinging jets have received increasing interests as flow pulsation is widely believed to increase heat transfer [5-24]. However, the existing investigations on the influence of pulsations on heat transfer under different flow and geometrical parameters show conflicting results. Both enhancement and no enhancement have been reported. Further studies are therefore warranted.

Many investigators have reported significant enhancement of heat transfer in pulsed impinging jets considering the possible features induced by the pulsations such as higher turbulence promoted by flow instabilities, increased entrainment by larger vortices, and non-linear dynamic response of the hydrodynamic and thermal boundary layers etc. [5-13]. Kataoka et al. indicated that the stagnation point heat transfer for axisymmetric submerged jets was enhanced by impingement of large-scale structures [5]. Zumbrunne et al. have reported a twofold enhancement of heat transfer in a planar impinging water jet with pulsation frequency in order of 100 Hz [6]. The experimental work shows that the enhancement depends on Reynolds number, impingement height, frequency, and amplitude of pulsations [6, 8, 9]. The tests by Sailor et al. show that the duty cycle representing the ration of pulse cycle on time to total cycle time has a significant effect on the heat transfer enhancement in an impinging air jet [10]. Camci et al. found strong increases in heat transfer at very large nozzle-to-plate distance (H/w = 24–60) and Reynolds numbers of 7500-14000 [11]. The measurements of heat transfer in circular air jet by Zulkifli et al. show that the stagnation point heat transfer doesn’t show any enhancement but the local heat transfer away from the stagnation point is significant enhanced for the higher turbulence intensity in this region [12, 13].

Some investigators only found a marginally beneficial effect of pulsation on heat transfer [14-18], Chaniotis et al. numerically studied the effect of jet pulsation on heat transfer and fluid dynamics characteristics of single and double jet impingement on a constant heat flux heated surface with the smooth particle hydrodynamics methodology, they stated the improvement of pulsation in the maximum temperature is not very large [15]. Behera et al. investigated the effect of sinusoidal- and square-wave pulsations on heat transfer by computational fluid dynamic (CFD), and show that the augmentation of the sinusoidal-wave pulsation which is less than 10% takes effect only for large amplitudes (>40%) [16]. The numerical results of Poh et al. on a 2-D planar impinging jet show that the heat transfer performance enhancement of both of laminar and turbulent pulsations is marginal [17, 18].

While many investigations indicate no enhancement of heat transfer or even show some deterioration of heat transfer as the pulsation energy mainly contributes to mixing between the jet and environment [19-24]. Fallen found no influence of pulsation on heat transfer in laminar flow, and only a slight increase or decrease in turbulent flow depending on frequency [19]. The experiments on cooling performance with an impinging water jet by Sheriff et al. where both of sinusoidal and square-pulse waveforms were used indicate that the reductions of local heat transfer by the sinusoidal pulsation decrease markedly from the stagnation point [20]. The investigation of Azevedo et al. on jet impingement with a rotating cylinder valve for a range of pulse frequency show that heat transfer degraded for all frequencies [21]. Mladin et al. reported a negligible increase (1%) in heat transfer in case of low amplitude and high frequencies and a decrease of heat transfer by the pulsation of up to 17% over a large range of frequencies, and they argued that high pulse frequency and low amplitude are better that low frequency and high amplitude [22, 23]. The examinations of axisymmetric impinging jets by Vejrazka also show no influence of pulsation on heat transfer [24].
Several researchers presented threshold values for effective pulsed impinging jet heat transfer [25, 26]. Mladin et al. reported a threshold Strouhal number (0.26), below which no significant heat transfer enhancement is obtained [25]. However, Sailor et al. still found significant enhancement in the stagnation point heat transfer for pulse flow at Strouhal number between 0.009 and 0.042 [10]. Recently, Hoffmann et al. investigated the influence of a pulsation on flow structure and heat transfer with experiments, and determined the threshold Strouhal number for small nozzle-to-plate distances to be in order of 0.2 [26].

Because of the complexity of flow structures and the non-linear dynamics in the boundary layer induced by pulsation, pulsed jet impingement flow and associated heat transfer has been a challenging problem and shown some intriguing aspects. The related physics for the pulsed jet impingement is not yet well-understood. Thus, the objective of this current study is to examine the influence of the sinusoidal pulsation on the heat and mass transfer in impinging jet by CFD method. The effect of Reynolds numbers and frequency as well as amplitude of the sinusoidal pulsation, temperature differences, and geometrical configuration will be discussed for further understanding of flow and thermal characteristics in pulsed impinging jet.

Mathematical model

As shown in fig. 1, a two dimensional symmetric slot impinging jet configuration will be numerically modeled. Due to geometric and flow symmetry, only the flow field within the half domain is solved. The fluid (air) was assumed to be incompressible and Newtonian with temperature-dependent fluid properties, and the viscous forces were negligible. Numerical simulation of the flow and thermal fields in a semi-confined turbulent impinging jet requires the solution of the continuity, eq. (1), the Navier-Stokes, eq. (2), and the energy eq. (3):

\[
\frac{\partial u_i}{\partial t} = 0
\]

\[
\frac{\partial (\rho u_i)}{\partial t} + \frac{\partial (\rho u_i u_j)}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} \left[ \mu \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \rho u_i u_j \right] + \rho g_i
\]

\[
\rho c_p \left( \frac{\partial T}{\partial t} + \frac{\partial (u_i T)}{\partial x_j} \right) = \frac{\partial}{\partial x_j} \left[ k \left( \frac{\partial T}{\partial x_j} - \rho c_p u_j T \right) \right]
\]

The Reynolds number based on the mean jet exit velocity \(u_{jet}\) and slot width \(w\) is \(Re = \frac{\rho u_{jet} w}{\mu}\). Many different turbulence models e.g. \(k-\epsilon\), \(k-\omega\), Reynolds stress, and \(v^2f\) model were used to model turbulent flow in steady impinging jets. The \(k-\epsilon\) model can only present reasonable agreement with experimental data for certain cases, as it cannot handle rapid length scale change and strong streamline curvature in the stagnation area, which can cause an anomalous turbulence production and lead to over-prediction of the heat transfer [27]. The \(k-\omega\) model has received attention in modeling turbulent impingement flows as it is easy to implement and often
predicts better results compared to those using the \( k-\varepsilon \) model [28]. The Reynolds stress model (RSM), taking anisotropy of the turbulence in the near-wall region account, has been shown to be superior to those \( k-\varepsilon \) and \( k-\omega \) models [29, 30]. The \( v^2f \) model has also indicated good agreement with a wide range of experimental results [31]. However, the \( v^2f \) model is more expensive as it requires resolution all the way to the wall without wall function approximation. In the present study, these four turbulence models will be firstly tested for sinusoidal pulsed turbulent impinging jet.

The following boundary conditions were used. A sinusoidal pulsation with flat velocity profile was applied at the inlet of the impinging jet as described below:

\[ u_{\text{jet}} = u_{\text{avg}} + A u_{\text{avg}} \sin(2\pi ft) \quad (4) \]

The jet flow and impingement surface were specified as isothermal, and the confinement wall was considered to be adiabatic; the uniform velocity, temperature, turbulent kinetic energy and energy dissipation rate profiles were assumed at the nozzle exit; no-slip condition was imposed at the impingement wall; the symmetry and fully developed outflow boundary conditions were taken at symmetry and outlet planes. The initial conditions \((t = 0)\) throughout the computational domain can be described as: \( u = v = 0, p = p_{\text{avg}}, \) and \( T = T_{\text{avg}}. \) The finite volume CFD code FLUENT 6.3 was used to numerically solve the flow and thermal fields in the pulsed turbulent impinging jet on a two dimensional symmetry domain. As the near-wall treatment is important in situations with heat and mass transfer near solid surfaces, thus, the boundary layer near the surface was kept in the order of \( y^+ \approx 1. \) Grid-independence of the final results was checked with different grid densities. Figure 2 shows the effect of grid size on the predicted time-averaged Nusselt number distribution. Typically, a grid density of 150 \( \times \) 50 provides satisfactory solution for the example shown. A second upwind discretization scheme was used considering the stability of solution convergence and the SIMPLEC algorithm was employed for the pressure-velocity coupling.

Results and discussion

The local Nusselt number for an isothermal impingement surface is conventionally defined as:

\[ \text{Nu} = \frac{q}{T_j - T_s} \frac{w}{k(T)} \quad (5) \]

The thermal conductivity of jet fluid \( k \) can be calculated according to different reference temperatures. Generally, the fluid conductivity calculated at jet temperature \( T_j, \) film temperature \( T_f = (T_j + T_s)/2 \) and impingement surface temperature \( T_s, \) and the corresponding Nusselt numbers are denoted by \( \text{Nu}_j, \text{Nu}_f, \) and \( \text{Nu}_s, \) respectively. The Nusselt number varies with time.
and position, therefore, the time-averaged local Nusselt number and time-averaged total Nusselt number can be, respectively, calculated by:

\[ \text{Nu}_{\text{avg}}(x, t) = \frac{1}{\Delta t} \int_0^{\Delta t} \text{Nu}(x, t) \, dt \]  

(6a)

\[\text{Nu}_{\text{avg}} = \frac{1}{A_0} \int_0^A \text{Nu}(x, t) \, dx \]  

(6b)

So far, most studies have involved small temperature differences between that of jet flow and target surface. Under small temperature differences, all fluid properties can be regarded as temperature-independent and the differences between the local Nusselt numbers calculated with thermal conductivity values at the jet, film, and impingement surface can be neglected. However, in some industrial applications such as fast paper drying and turbine blade cooling, very high temperature and large temperature difference which involve temperature-dependent thermophysical properties are used to obtain very high heat transfer rates. The study of Shi et al. on steady turbulent slot impingement jet involving temperature differences ranging from 12 to 272 °C indicates that large temperature differences lead to significant differences in the heat transfer coefficients [32]. It is therefore necessary to compare local Nusselt number with the three definitions in pulsed impinging jet under large temperature differences.

Model validation

Since few investigations have been conducted on the predictive ability of various turbulence models for pulsed turbulent impinging jets, four turbulence models frequently used for steady turbulent impinging jets: standard \( k-\varepsilon \) model, \( k-\omega \) model, RSM, and \( v^2f \) model were tested for sinusoidal pulsed turbulent impinging jet for a cooling application. The time-averaged Nusselt number calculated at the film temperature \( \text{Nu}_f \) was used to validate present mathematical models; the film temperature is usually adopted in experimental calculations [9]. Figure 3(a) shows a comparison between the numerically predicted local time-averaged Nusselt number \( \text{Nu}_f \) distributions and that of pulsed and steady impinging jet experi-

![Figure 3. Comparison of numerical results with experimental results [9] at \( H/w = 5 \)](image)

(a) turbulence model test at \( H/w = 5, Re = 5500, A = 17\% \), and \( f = 41 \, \text{Hz} \); (b) predicted Nusselt number distribution with RSM at \( Re = 1000 \) \( (A = 12\%, f = 23 \, \text{Hz}) \), \( 5500 \) \( (A = 17\%, f = 41 \, \text{Hz}) \), and \( 11000 \) \( (A = 25\%, f = 41 \, \text{Hz}) \) (color image see on our web site)
ments for $H/w = 5$ and $Re = 5500$. It can be seen that the RSM predicts better local Nusselt number distribution at amplitude $A = 17\%$ and frequency $f = 41$ Hz. Figure 3(b) shows a comparison between the numerically predicted time-averaged Nusselt number $Nu_f$ distributions by RSM with that of pulsed impinging jet experiments under $H/w = 5$ and $Re = 1000, 5500$, and 11000. Considering the relatively large relative error of the experiments (9.6%, 10.6%, and 12% for $Re = 1000, 5500$, and 11000, respectively), the RSM can capture the overall shape of the Nusselt number distribution relatively well. The RSM model can make reasonable prediction near the stagnation point but slightly overestimates the magnitudes of Nusselt number in the wall jet region. Thus, this model is therefore deemed acceptable for subsequent simulation runs.

**Parametric study for cooling case**

For the cooling case, the temperature of jet flow is set as $T_4$, and the temperature differences between the jet flow and that of impinging surface range from 50 to 400 K. The effects of Reynolds number ranging from 5500 to 25000, frequency from 20 to 80 Hz and amplitude from 5 to 50% as well the nozzle-to-plate distance ranging from 3 to 8 are discussed for further understanding of the flow and thermal characteristics in pulsed turbulent impinging jets under large temperature differences and to examine the effect of pulsation on heat transfer.

![Figure 4. Local Nusselt number distributions under $H/w = 5$, $Re = 5500$, $A = 17\%$, and $f = 41$ Hz with different reference temperature (color image see on our web site)](image-url)
Figure 4 indicates three possible local Nusselt numbers at large temperature differences between impinging jet and impingement surface of $\Delta T = 50$ K, $\Delta T = 100$ K, $\Delta T = 200$ K, and $\Delta T = 400$ K, respectively. In the cooling case, as the jet flow temperature is lower than that of the impingement surface, the time-averaged Nusselt number with jet temperature is larger than that with film temperature which is larger than that with impingement surface temperature, $\text{Nu}_j > \text{Nu}_f > \text{Nu}_s$. At a low temperature difference, $\Delta T = 50$ K, the three time-averaged Nusselt numbers are as expected close to each other and the maximum difference between $\text{Nu}_j$ and $\text{Nu}_s$ is within 10% which can be approximately neglected, fig. 4(a). However, the difference between the three Nusselt numbers increases as the temperature difference increases. For example, at large temperature difference $\Delta T = 400$ K, $\text{Nu}_j$ is even two times larger than $\text{Nu}_s$. Figure 5 shows the distributions of local time-averaged Nusselt number at film temperature under various temperature differences between the jet flow and impingement surface. It is clear that the larger of the temperature difference, the smaller of the time-averaged Nusselt number. Negligible difference between pulsed and steady impinging jet is obtained even at large temperature difference.

The effect of the mean jet Reynolds number on time-averaged Nusselt number is portrayed in fig. 6, where it can be observed that increasing Reynolds number enhances heat transfer in pulsed impinging jet. Under the present conditions ($H/w = 5$, $\Delta T = 100$ K, $A = 17\%$, $f = 41$ Hz) and Reynolds number ranging from 5500 to 25000, almost no enhancement on heat transfer can be found that is attributable to pulsation. Even at different amplitudes and frequencies of pulsation, the effect of pulsation on heat transfer in impinging jet is not appreciable (fig. 6).
7). Figures 7(a) and (b) indicate that the effects of amplitude and frequency on the time-averaged local Nusselt number distribution are very small, even negligible. Further calculation indicates that a scaling law can be found between the time-averaged total Nusselt number and Reynolds number as $N_{\text{u,ave}} \sim Re^{0.74}$, and the time-averaged local Nusselt number at stagnation point ($x/w = 0$) relates with Reynolds number as $N_{\text{u,0}} \sim Re^{0.55}$ at $H/w = 5$, and $\Delta T = 100$ K.

Figure 8 shows the time-averaged Nusselt number distribution for various nozzle-to-plate spacings. It can be seen that the geometry of the impinging jet has important effect on its heat and mass transfer performance. It is clear from fig. 8 that the local Nusselt number near the stagnation point increases as nozzle-to-plate distance increases, which is consistent with the experimental data [9].

**Parametric study for heating case**

The temperature of the impingement surface is taken as $T_\text{s}$, while the jet flow temperature is much larger than that of impingement surface for heating. Numerical calculations were performed for heating cases to investigate the effect of pulsation on heat and mass transfer. The parameters considered are temperature differences ($50 \text{ K} \leq \Delta T \leq 400 \text{ K}$), mean jet Reynolds numbers ($1000 \leq Re \leq 11000$), pulsation amplitude ($5\% \leq A \leq 50\%$) and frequency ($20 \text{ Hz} \leq f \leq 60 \text{ Hz}$), as well as nozzle-to-plate distance ($3 \leq H/w \leq 10$). In the heating cases, as the jet flow temperature is larger than that of the impingement surface, Nusselt number at jet temperature is lower than that at the film temperature which is in turn smaller than that at impingement surface temperature, $N_{\text{u,j}} < N_{\text{u,f}} < N_{\text{u,s}}$. The numerical calculations show that reduced temperature difference and increased Reynolds number can both enhance the time-averaged local Nusselt number (fig. 9), which is similar to that observed for the cooling case. Furthermore, no evident enhancement of
heat transfer by pulsation can be found for the heating case as well. At $H/w = 5$ and $\Delta T = 50$ K, the time-averaged local Nusselt number at stagnation point ($x/w = 0$) and the time-averaged total Nusselt number show scaling laws as $\text{Nu}_0 \sim \text{Re}^{0.71}$ and $\text{Nu}_{\text{ave}} \sim \text{Re}^{0.76}$ with Reynolds number, respectively. Figure 10 shows the time-averaged Nusselt number distribution for different nozzle-to-plate spacing. It can be observed that the geometry of the impinging jet has an important effect on its heat and mass transfer. It is clear from fig. 10 that the Nusselt number decreases with increase of nozzle-to-plate distance, which is opposite to that of the cooling case.

**Concluding remarks**

The effects of large temperature differences, mean jet Reynolds number, frequency, and amplitude of pulsation as well as the nozzle-to-plate distance on heat transfer in impinging jet are studied for both cooling and heating applications, respectively. The numerical results show that the local time-averaged Nusselt numbers calculated with various thermal conductivity values at the jet, film, and impingement surface temperatures in both cooling and heating cases differ significantly for large temperature differences (>100 K). The temperature difference and Reynolds number have significant influence on heat transfer under pulsed turbulent impinging jets. Increased temperature differences can reduce the Nusselt number, whereas increasing Reynolds number results in Nusselt number enhancement. The results indicate that the local Nusselt number at stagnation point and the averaged Nusselt number correlate with the mean jet Reynolds number with similar scaling laws. The Nusselt number increases with increase of nozzle-to-plate distance near the stagnation point in cooling case, which is opposite to
that of the heating case. No obvious enhancement by single pulsation can be found under current conditions except for cases with large temperature differences at distance far from stagnation point.

**Acknowledgments**

This work was jointly supported by China Scholarship Council and National Natural Science Foundation of China through Grant number 10947153 and 10802083.

**Nomenclature**

- \( A \) – amplitude of pulsation, [%]
- \( c_p \) – specific heat, [Jkg\(^{-1}\)K\(^{-1}\)]
- \( f \) – frequency of pulsation, [Hz]
- \( g \) – gravity acceleration [ms\(^{-2}\)]
- \( H \) – nozzle-to-plate spacing, [m]
- \( k \) – thermal conductivity, [Wm\(^{-1}\)K\(^{-1}\)]
- \( L \) – jet length, [m]
- \( Nu \) – Nusselt number, eq. (5)
- \( Pr \) – Prandtl number (= \( \frac{m c_p}{k} \))
- \( p \) – static pressure, [Pa]
- \( q \) – heat flux, [Wm\(^{-2}\)]
- \( Re \) – Reynolds number (= \( \frac{\rho u_{jet} w}{m} \))
- \( T \) – temperature, [K]
- \( \Delta T \) – temperature difference, [K]
- \( t \) – time, [s]
- \( u, v \) – velocity component in x- and y-directions, [ms\(^{-1}\)]
- \( w \) – slot width, [m]
- \( x, y \) – Cartesian co-ordinates, [m]
- \( y^+ \) – dimensionless distance between the wall and the first node

**Greek symbols**

- \( \rho \) – density, [kgm\(^{-3}\)]
- \( \mu \) – dynamic viscosity, [kgm\(^{-1}\)s\(^{-1}\)]

**Subscripts**

- \( \text{avg} \) – average
- \( i, j \) – indices in Einstein summation
- \( j \) – jet flow
- \( \text{jet} \) – jet inlet
- \( f \) – film temperature
- \( s \) – impingement surface
- \( 0 \) – stagnation point
- \( ' \) – fluctuation

**References**

tions on Heat Transfer Enhance-


[32] Shi, Y. L., Ray, M. B., Mujumdar, A. S., Effect of Large Temperature Differences on Local Nusselt Num-
ber under Turbulent Slot Impingement Jet, Drying Technology, 20 (2002), 9, pp. 1803-1825