An experimental study was conducted to investigate the influence of Reynolds number and equivalence ratio on flame temperature field and thermal flame height of laminar premixed landfill gas fuel. Mach-Zehnder interferometry technique is used to obtain an insight to the overall temperature field. The slot burner with large aspect ratio, length of 60 mm and width of 6 mm, was used to eliminate the three-dimensional effect of temperature field. Two kinds of mixed fuels, LFG70 (70% CH4-30% CO2 on volume basis) and LFG50 (50% CH4-50% CO2) were used to investigate flame characteristics under the test conditions of 100 ≤ Re ≤ 600 and 0.7 ≤ φ ≤ 1.3. The present measurement reveals that the variation of maximum flame temperature with increment of Reynolds number is mainly due to heat transfer effects and is negligible. On the other hand, the equivalence ratio and fuel composition have a noticeable effect on flame temperature. In addition, the results show that the landfill gas flames compared to the CH4 ones have a lower flame temperature. With increment of CO2 volume fraction at lean combustion, thermal flame height is augmented while at stoichiometric and rich combustion, its value reduced. Thermal flame height augments linearly by Reynolds number increase, while its increment at rich mixture is higher and the effect of Reynolds number at lean mixtures is insignificant. For validation of experimental results from Mach-Zehnder Interferometry, K-type thermocouples are used at peripherally low and moderate isotherm lines.

Key words: temperature profile, laminar flame, premixed LFG/air, slot burner, Mach-Zehnder interferometer

Introduction

Due to the diminution of fossil fuel supplies and increment of energy expenditure, the combustion of renewable fuels derived from biomass became gradually important [1]. Landfill gas (LFG) is a kind of biogas, produced by bacterial decomposition, volatilization, and chemical reaction of animal and other type of solid waste [2]. The raw materials can be municipal waste, green waste, plant material, and crops. In the late of 1980s, it was found that LFG is flammable and can be used as a fuel for generating electricity, domestic, and industrial purposes [3].

LFG mostly consists of CH4 and CO2 and small amounts of oxygen and nitrogen. The methane volume fraction has a ranging from 50% to 70% that pertains to its formation procedure [4]. Since concentration of carbon dioxide is high, heating value, flame stability, burning velocity and flame temperature are less than other hydrocarbon fuels [5].
Many investigations have been done in order to solve these problems. Lee et al. [6] studied the effect of mixing fuels to increase heating value and flame stability of LFG fuel. It was observed that by addition of liquefied petroleum gas (LPG), the heating value and flame stability of mixed fuel was increased, and LFG-LPG can be substituted instead of LFG in domestic combustion appliances. Dai et al. [7] investigated the flame stability of premixed biogas flame for reference test burner. Six combustible mixtures were selected and used to study the flame stability in which the CO2 volume fraction varies in the ranges of 30% to 45%. It was shown that by increasing primary air ratio and CO2 volume fraction and the lifting limits reduced while the yellow tipping limits enhanced. The effect of hydrogen addition on flame characteristics of biogas in Bunsen burner was studied by Zhen et al. [8]. The three biogas composition, BG60 (60% CH4-40% CO2 on the volume basis), BG50 and BG40 were chosen and the fraction of hydrogen in the biogas mixtures varies in the range of 10% to 50%. The Reynolds number was selected within the ranges of 400 ≤ Re ≤ 800 and equivalence ratio of 0.8 ≤ φ ≤ 1.2. It was shown that by increments of the hydrogen fractions in fuel mixture, the flame characteristics such as flame stability, laminar burning velocity and flame temperature were augmented. Cardona et al. [9] investigated the effects of propane and hydrogen addition on biogas (66% CH4-34% CO2) experimentally and numerically. For numerical study, the GRI-Mech 3.0 and C1-C3 reaction mechanisms were used. It was shown that by addition of propane and hydrogen, the burning velocity significantly elevated. It was also discerned that for biogas/propane/hydrogen mixture, burning velocity reaches to its maximum at equivalence ratio, φ = 1, whereas it occurs at φ = 1.1 for biogas. Liu et al. [10] obtained the structure and laminar burning velocity of pyrolysis gases, landfill gases and syngas gases (mixture of CO and H2) numerically. The flame temperature, burning velocity and species mass fraction of fuel mixtures obtained from the reaction zone. There was a difference between the stoichiometric methane/air flame and LFG50/air flame, and it was discovered that flame temperature and emission of landfill combustion is less than methane combustion.

Landfill gas is reachable in remote rural area and environmentally friendly renewable fuel. The heating value of Landfill gas for domestic combustion appliances and electricity generation satisfies the need. The present work was implemented to study the flame characteristics of LFG50 (50% CH4-50% CO2) and LFG70 (70% CH4-30% CO2) fuels and compared with the results of methane/air flame [11] in a slot burner. Temperature value and its distribution depend highly on equivalence ratio and Reynolds number of the unburned combustible mixture. The variation in the equivalence ratio, which leads to a rich and lean mixture, changes the flame temperature and increasing the Reynolds number reforms the structure of the flame. Hence, evaluation of temperature distribution of flame in different states is what we need for a desirable burner design [12]. Equilibrium concentration, emission characteristic and species reaction rate are all related to regional flame temperature [13]. It is essential to obtain the heat transfer rates of combustion processes to investigate the temperature field of the premixed flames [14].

Many experimental methods for temperature measurements have been implemented. Most of the practical techniques are achieved by thermocouple and resistance thermometers [15]. These methods are intrusive, point wise and disturb the temperature field of the region of interest. Optical methods are mainly fast, non-intrusive and accurate [16]. Many optical methods such as Interferometry, Laser speckle technique, Schlieren photography and Moire deflectometry have been examined to observe temperature field of gaseous flames. All the interferometry methods, including Mach-Zehnder interferometry, Talbot interferometry and Holographic interferometry are based on changes in the refractive index of the gaseous products of the flame. By knowing the flame gaseous products and using the Gladstone-Dale relation, the temperature
can be calculated [17, 18]. For a premixed flame, the error resulted from diversity in gas composition is less than 2% for equivalence ratio of, \( \phi < 2 \) [19, 20]. Therefore, the refractive index of air can be substituted instead of gaseous products of combustion [21].

Laminar premixed LFG flame in a slot burner has rarely been studied. In order to determine the heat transfer rate of combustion processes, it is necessary to obtain temperature field of the premixed flame. Present work is done to obtain temperature profile, thermal flame height and visualize the temperature field of two LFG mixtures (LFG\textsubscript{50} and LFG\textsubscript{70}) at different equivalence ratios and Reynolds numbers.

**Experimental procedure**

**Interferometer**

Flame structure and temperature field of laminar premixed methane/air combustion is captured using Mach-Zehnder interferometry (MZI) which is a non-intrusive method. A schematic of the interferometer setup is shown in fig. 1. The interferometer consists of a 10 mW Helium-Neon laser with 632.8 nm wavelength, two doublets, a pinhole, a micro-lens, three flat mirrors (M), two beam splitters (BS) and a CCD camera. The mirror and the Beam Splitters are at parallel position to facilitate the infinite fringe mode. More details about Mach-Zehnder interferometry technique is presented in the literature [22, 23]. All the isotherm patterns are captured by an “ARTCAM-320p” 30 fps CCD camera with 3.2 M pixels, which is connected to a PC to record the images.

**Experimental set-up**

The layout of the experimental set-up is depicted in fig. 2. Flame was generated using a stainless-steel rectangular burner with an inner cross-section of 60 mm × 6 mm and 250 mm height and wall thickness of 3.5 mm. Length to width ratio of the burner is large enough to eliminate three-dimensional effects of flame in z-direction.

In order to obtain a uniform exit velocity profile, the inside surface of the slot burner is highly polished. Furthermore, 1.5 mm diameter stainless-steel balls and a honeycomb section were used at the mixture entrance to the burner in order to prevent non-uniformity of the flow. The geometrical detail of the burner is illustrated in fig. 3. The slot burner is mounted on a positioner which can move both horizontally and vertically to achieve the parallelism of the laser beam with the slot burner length. In order to protect the flame from ambient disturbance, the burner is surrounded by an enclosure with cross-section of 25 cm × 50 cm and height of 150 cm. The enclosure is made up of transparent plexiglas with 5 mm thickness that enables the visualization of the flame structure. Two 10 cm in diameter windows are mounted on the enclosure’s walls to let the laser beam pass through the test section.

The CH\textsubscript{4} and CO\textsubscript{2} gases are contained in high pressure cylinders and have over 99.9% purity. The fuels pressure are controlled by two pressure regulating valve. A compressor is used to supply air to the mixer.
The flow rates are measured by three rotameters that each are specifically calibrated for CH₄, CO₂ and air. The calibrated rotameters have an error of 3% of the flow rates at operating conditions. A brass cylindrical mixing chamber filled with stainless-steel balls is utilized to premix the fuel and oxidizer. All the temperatures are recorded using K-type thermocouples and a “TESTO 177” four-channel data logger, which is connected to a PC. All the thermocouples were calibrated in an isothermal bath. In order to prevent the flame flashback in the tube and cylinders, two flashback arrestors are utilized. Further details can be found in fig. 2.

**Data reduction**

The objective of data reduction procedure in this study is to specify the temperature field of the laminar premixed flame in the slot burner. A code has been developed to obtain the temperature field and isotherm patterns at different Reynolds numbers and equivalence ratios.

When a laser beam crosses through a hot medium, an optical path difference occurs due to the changes of the refractive index in the medium. The optical path difference of two beams separated by the first Beam Splitter (BS1) can be obtained [24] as:

\[
\epsilon = \frac{1}{\lambda_0} \int d \left[ n_{ad} - n(x, y, z) \right] dz \tag{1}
\]
where $\lambda_0$ is the wavelength of the laser beam that equals to 638.2 nm, $n_{\text{ref}}$ is the refractive index of the air at reference state and $n(x,y,z)$ is the local refractive index of the flame. $L$ is the characteristic length of the burner along the light beam.

In order to obtain reference refractive index the ambient temperature, pressure and relative humidity are required to be measured. As mentioned before, the burner’s cross-section dimensions assure two-dimensional assumption and since changes of refractive index in $z$-direction is negligible. Therefore, eq. (1) is simplified to:

$$\varepsilon = \frac{n_{\text{ref}} - n(x,y)}{\lambda_0} L$$

(2)

The local refractive index is obtained:

$$n = n_{\text{ref}} - \frac{\varepsilon \lambda_0}{L}$$

(3)

By determining the local refractive index from eq. (3), Gladstone-Dale equation [25] calculates the local temperature:

$$T(x,y) = \left[ \frac{n_{\text{ref}} - 1}{n(x,y) - 1} \right] T_{\text{ref}}$$

(4)

where $T_{\text{ref}}$ is the temperature of the undisturbed region near the flame. Equation (4) gives temperature in a specific point of a fringe and since each fringe represents an isotherm, the temperature of the overall fringe is obtained. In this study, twenty photographs were captured to ascertain the reliable fringe patterns at each specific Reynolds number and equivalence ratio. The Reynolds number of slot flame burner was measured corresponding to cold fuel/oxidizer mixture gasses and defined [26]:

$$\text{Re} = \frac{\rho_{\text{mix}} V_{\text{exit}} D_h}{\mu_{\text{mix}}}$$

(5)

where $\rho_{\text{mix}}$ is the density of the gaseous mixture, $\mu_{\text{mix}}$ – the dynamic viscosity of mixture, $D_h$ – the hydraulic diameter and $V_{\text{exit}}$ – the velocity at exit from the slot burner.

The $\mu_{\text{mix}}$ and $D_h$ are calculated as follows:

$$\mu_{\text{mix}} = \frac{\sum (\mu_i Y_i \sqrt{M_i})}{\sum (Y_i \sqrt{M_i})}$$

(6)

$$D_h = \frac{4LW}{2(L+W)}$$

(7)

where $i$ represents the mixture component, $Y_i$ is the mole fraction, $M_i$ – the molecular weight, $L$ and $W$ are the slot length and width, respectively.

Reliability of experimental results

Uncertainty analysis

The uncertainties of the obtained flame temperature are evaluated from three major sources: the uncertainty of equivalence ratio ($\phi$), uncertainty of Reynolds number and the uncertainty of optical method. The uncertainties in equivalence ratio and Reynolds number
are mainly due to uncertainties in the volumetric flow meters of fuel and oxidizer. The uncertainty analysis has been carried out for all the cases. The maximum uncertainties are ±12.7% and ±3.46% for equivalence ratio and Reynolds number, respectively. Detail information about measurement of this uncertainty is presented in [27, 28].

The other source of uncertainty arises from Mach-Zehnder interferometer. Since the refractive index of air is considered as that of the combustion products, it is one of the error sources. The average error for this case is 2.3% at the equivalence ratio of 2 [29] and at the lower equivalence ratio, the error is less than 2% [30].

The second cause for errors in the optical method is changes in the refractive index of air at high temperatures. When the laser beam passes through a premixed slot flame jet, will deviate from its original path. Kharitonov [31] suggested that for temperatures up to 6000 K the variation of air refractive index is negligible and can be considered to that of the air refractive index under normal condition. The last source of error can be due to the constant property assumption for the fuel and air. It was shown that the maximum error for this consideration is less than 3% [32].

Validation

In order to investigate the accuracy of the experimental results and data reduction method, the temperature obtained from the optical method is compared with that of thermocouples at the horizontal line passing through the center of maximum temperature region. The measured flame temperatures with thermocouples were modified to account for the effect of convection and radiation [33]. Figure 4 shows the comparison of the results obtained from the two experimental method at Re = 300 and equivalence ratios of 0.7 and 1 for LFG and LFG50. Good agreement is obtained between the flame temperature profiles using interferometry compared against the results of thermocouples. Regarding to the thermocouple kind (K type), the validation for higher temperatures than 1400 K was impossible. The maximum discrepancy between the temperature obtained from thermocouples and Mach-Zehnder interferometry technique is 23 °C and 27 °C for the equivalence ratio of 0.7 and 1, respectively.

Results and discussion

The effects of Reynolds number and equivalence ratio on the thermal flame height ($H_T$), flame temperature and structure of LFG flames are studied experimentally with the inlet condition of $T_0 = 298$ K and $P_0 = 0.87$ atm. In the present study, the effect of Reynolds number ranging from 100 to 600, which is in the laminar flame region, and equivalence ratios of $\phi = 0.7, 1$ and 1.3 are investigated.

Flame structure

The flame structure of the premixed LFG fuel at equivalence ratio of, $\phi = 1.3$, Reynolds number of 400 and LFG50 fuel at equivalence ratio of unity and Reynolds number of 200
is characterized in fig. 5. According to fig. 5(a), the flame contains three major zones: inner zone of unburned gases, luminous zone of hot radical species and outer zone, which contains mainly complete combustion products. Isotherm lines of corresponding regions in flame zone with their temperature values are presented in fig. 5(b). In this figure, some of the isotherm lines were skipped for clarity. The greatest temperature gradient occurs along the boundary of the inner zone. It is also observed that the maximum temperature occurs just above the inner zone. This vertical distance, from the burner to end of the inner zone, define as thermal flame height ($H_T$), which indicated in fig. 5(a). Another region of the large temperature gradient is observed at the outer boundary of the flame, where heat is lost rapidly to the low temperature surroundings.

**Effects of Reynolds number and equivalence ratio**

Effect of Reynolds numbers of 400 and 600 at different equivalence ratios of 0.7, 1, and 1.3 on structure of the laminar premixed LFG $N_0$/air flame is illustrated in fig. 6. As is depicted, by increasing the Reynolds number, the height of the inner zone, which is an indicator of thermal flame height, augments. In fact, the thermal flame height is proportional to Reynolds number. Since Reynolds number is proportional to the inlet average velocity at each equivalence ratio, increasing Reynolds number causes the reaction zone to occur at higher vertical distances.

At lean combustion due to existence of further air, the fuel consumption rate is higher and mixture devours right after escaping from the burner. As air to fuel ratio decreases to the rich values, mixture will need extra air for complete combustion, which leads to flame stretch. Consequently, a longer vertical distance is required for fuel to burn completely, and length of the inner zone will be larger than lean flames. Figure 6 also demonstrates that the effect of Reynolds number on height of the inner zone is more pronounced than the equivalence ratio.

By shifting from lean to rich mixture, the inner zone of unburned gas stretches and the maximum flame temperature area is enhanced but stability of the flame is decreased. The problem of flame stability is due to air suction by the flame, which causes unwanted cross flow and flame
oscillation. Because the structure of the methane and LFG70/air flame is similar to the LFG50/air flame, to avoid repetition, their isotherm patterns are not shown throughout this paper.

Flame temperature

Figure 7 illustrates flame temperature profiles of premixed methane [11], LFG70 and LFG50/air flames at Re = 400 and equivalence ratio of unity at a horizontal line which passes through the center of the maximum temperature isotherms. It is observed that at the same level of x, the temperature of methane/air combustion is higher than those of the LFG70/air and LFG50/air flame. This figure reveals a trend that the higher CO2 concentration in the LFG, the lower the flame temperature. This is because the CO2 is an inert gas. The presence of CO2 in the LFG dilutes the hot combustion gases during the burning process of the fuel, and these diluents would simply absorb heat from the combustion process. In addition, the CO2 gas is a good radiation emitter, and thus the radiation energy loss tends to be larger in the flame diluted by CO2, further contributing to its lower temperature. The maximum temperature of stoichiometric of methane flame is 2111 K, which is 0.91 of adiabatic flame temperature. The difference is mainly due to heat transfer effects and air suction from the periphery medium. This figure also points out that the maximum temperatures of LFG70 and LFG50 are 1949 K and 1889 K, respectively. Although the LFG fuel includes about 30% and 50% of inert gas such as CO2 for LFG70 and LFG50, the flame temperature get relatively as high as 1850 K at stoichiometric condition.

Figure 8 shows the distribution of temperature in the reaction zone for the lean and rich LFG flames. The temperature profile of LFG50 flame also show a similar trend to that of the LFG70 flame expecting that the maximum temperature value of LFG70 is slightly higher than LFG50. At lean combustion, φ = 0.7, in the same level of x, the flame temperature of LFG70 is higher than LFG70 while maximum flame temperature of LFG70 is 50 K higher than LFG50. At rich condition, φ = 1.3, temperature of LFG70 is almost higher than LFG50 in all horizontal locations.

Maximum flame temperature of methane, LFG70 and LFG50 at φ = 1 and Re = 400

Maximum flame temperature of methane, LFG70 and LFG50 at different equivalence ratio ranging from 0.7 to 1.3 is shown in fig. 9. The figure shows that the flame with φ = 1 has the highest temperature among all the flames within 0.7 ≤ φ ≤ 1.3. It is simply because relatively more complete combustion occurs at φ = 1 than other equivalence ratios. As the flame becomes richer, incomplete combustion occurs and results in monotonically lower temperature at higher
equivalence ratios. At lean combustion, due to further air, the fuel consumption rate is high and the extra air which does not participate in the combustion processes causes to lower flame temperature. The figure also shows that the methane flame has a higher temperature than the LFG fuels due to the lower LHV in the LFG gas flame.

In fig. 10 the maximum flame temperature obtaining from data reduction is shown at different Reynolds numbers and equivalence ratios. Although by increasing the Reynolds number, heat flux is enhanced, but the maximum flame temperature change is negligible. At the constant equivalence ratio of unity, by increasing Reynolds number from Re = 100 to 600, the maximum temperature difference of 35 K is observed.

Flame temperature of LFG\(_{50}\) fuel along the horizontal line passing through the maximum temperature point at different Reynolds number at stoichiometric condition are shown in fig. 11. By increasing Reynolds number flame expands and a greater area is affected by heat flux from combustion zone. These results show that LFG has a sufficient potential as alternative fuel with respect to flame temperature and may be utilized usefully in various types of combustion equipment.

**Thermal flame height**

The thermal flame height is considered as an important parameter in characterizing the structure of premixed flames. Thermal flame height \((H_T)\) defined as the vertical distance from the burner at which the temperature is maximized [34], occurs just above the inner zone [35].

Thermal flame height for Reynolds number ranging from 100 to 600 and equivalence ratio of 0.7 is illustrated in fig. 12. It is observed that the thermal flame height enhanced almost linearly with increment of Reynolds number up to 400, and after that, its increment becomes insignificant. The change in thermal flame height is around 76.19\%, 98.66\%, and 118.9\% for CH\(_4\), LFG\(_{70}\) and LFG\(_{50}\), respectively. By increasing CO\(_2\) thermal flame height is augmented at lean combustion.

Thermal flame height at equivalence ratios of, \(\varphi = 1\) and \(\varphi = 1.3\) are shown in figs. 13(a) and (b), respectively. The changes in thermal flame height is about 371.78\%, 285.36\%, and 280.36% at \(\varphi = 1\) and 326.12%, 323.31% and 307.13% at \(\varphi = 1.3\) for CH\(_4\), LFG\(_{70}\) and LFG\(_{50}\), respectively. Despite the lean combustion, at stoichiometric and rich combustion, by increasing the CO\(_2\) thermal flame height reduced. The thermal flame heights of LFG fuels also
show a similar trend to that of CH\(_4\) and their relationships are linearly with Reynolds number increment. As shown in figs. 12 and 13, by increasing equivalence ratio from \(\phi = 0.7\) to \(\phi = 1.3\), the thermal flame height is increased and the tip of the flame cone moves upward. Therefore, the effect of an increase in the equivalence ratio is to reduce the maximum flame temperature and meantime move the location of the maximum temperature region upward.

**Conclusions**

The Mach-Zehnder interferometry technique as an accurate and nonintrusive method is utilized to measure and visualize the two-dimensional laminar LFG flames. Good agreement is observed between optical method and thermocouples results, which show its ability to be used instead of other experimental methods. Three major regions are observed in flame, which clearly characterizes its structure, flame height and reaction zone. The effects of Reynolds number ranging from 100 to 600 and equivalence ratio ranging from 0.7 to 1.3 on isotherm lines
and temperature profiles are studied experimentally and the results of the present investigation are summarized as follows.

- The results show that by increasing Reynolds number, the height of the inner zone is augmented and the peak of the flame temperature occurs at a higher vertical distance. In addition, by increments of Reynolds number flame expands and a greater area is heated, but variation in maximum gas temperature is negligible.

- The effect of gas composition on thermal flame height ($H_T$), structure, temperature profile and isotherm lines is studied experimentally. By increasing inert gas such as CO$_2$, the flame temperature and thermal flame height at rich combustion are reduced; while at lean combustion, thermal flame height is augmented. In addition, the results indicate that the thermal flame height enhanced almost linearly with increment of Reynolds number at each equivalence ratio.

- The effect of Reynolds number on thermal flame height at stoichiometric and rich combustion is more pronounced than the lean combustion. By increasing or decreasing equivalence ratio due to incomplete combustion, the flame temperature and its stability are reduced.

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